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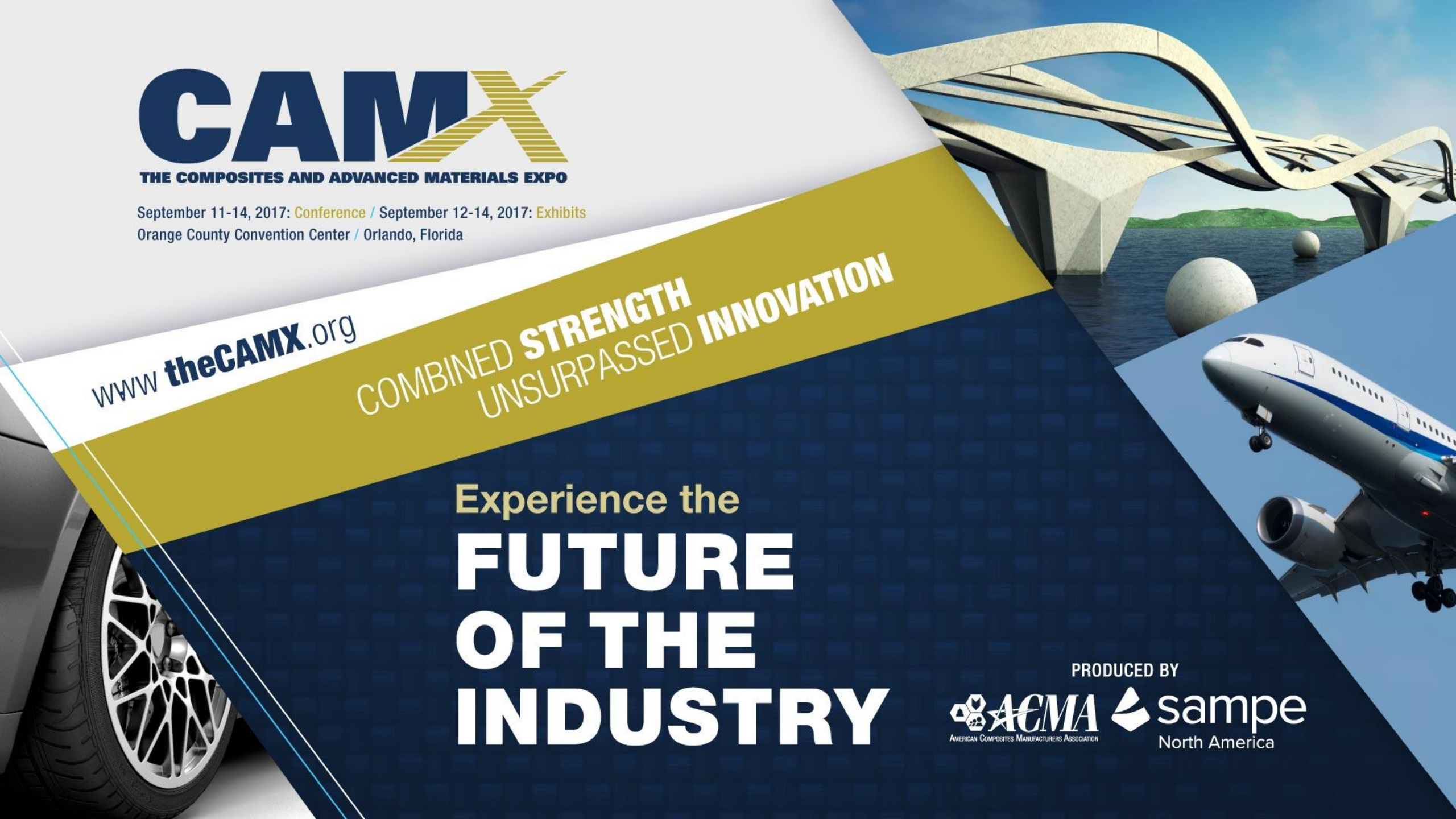
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Tow-Path Based Modeling of Wrinkling during the Automated Fiber Placement Process

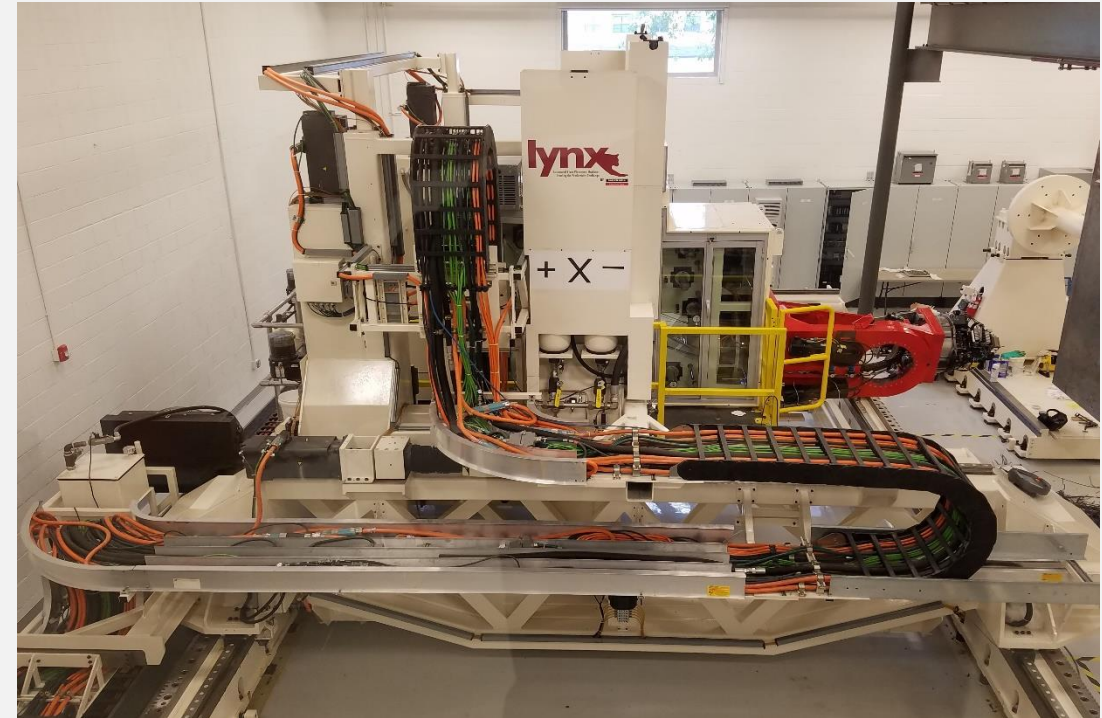
Roudy Wehbe, Brian F. Tatting, Ramy Harik, and Zafer Gürdal
University of South Carolina, Ronald E. McNair Center

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The Boeing Company



Introduction

- AFP machines are used to manufacture large aerospace structures.
- Typical material that is laid down using AFP machines have a width of $\frac{1}{8}$ in, $\frac{1}{4}$ in, or $\frac{1}{2}$ in.
- AFP delivers up to 32 tows in a single sequence to form a course, while a sequence of courses is termed ply.
- During the process, the layup speed, temperature, roller compaction, and tow tension are controlled to obtain a good layup quality.
- Some defects might appear during the process, such as wrinkling, tow twisting, folding, missing tows, and others...



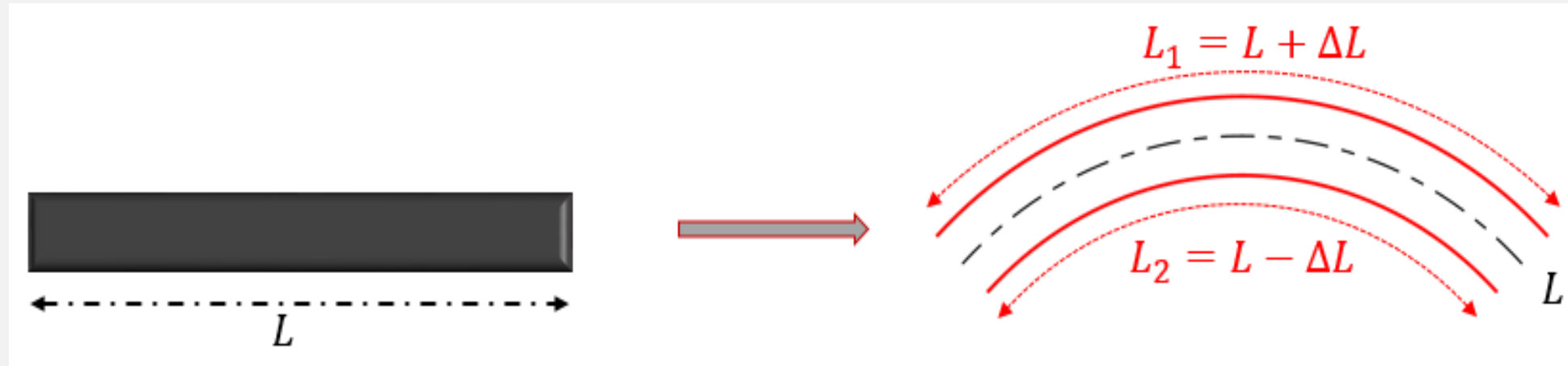
AFP machine at the McNair Center



AFP machine head
with 32 tows [1]

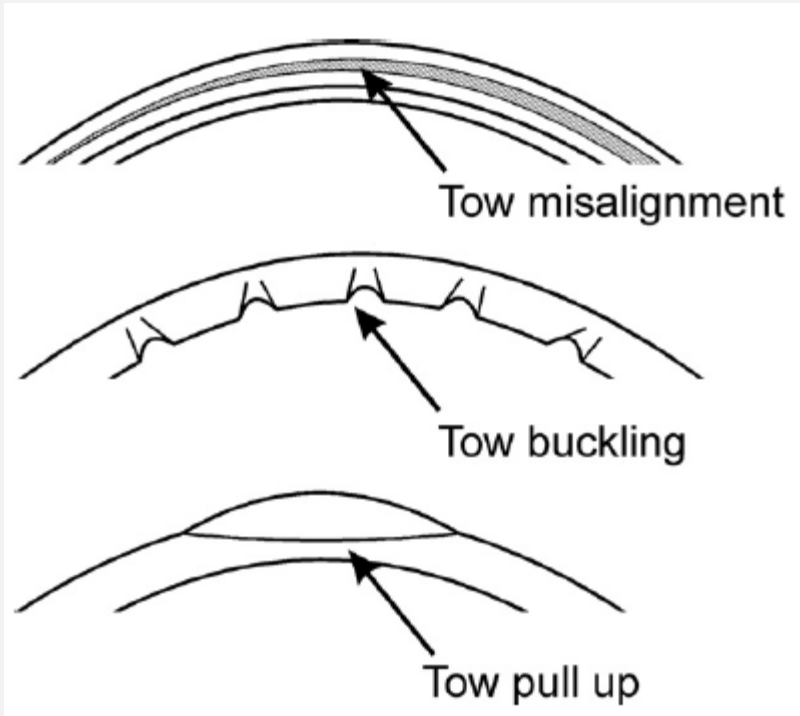
[1] Beakou, A., Cano, M. & Le Cam, J. B., "Modeling slit tape buckling during automated prepreg manufacturing: A local approach." *Composite Structure* 93 (2011): 2628-2635

Origin of Wrinkling in AFP

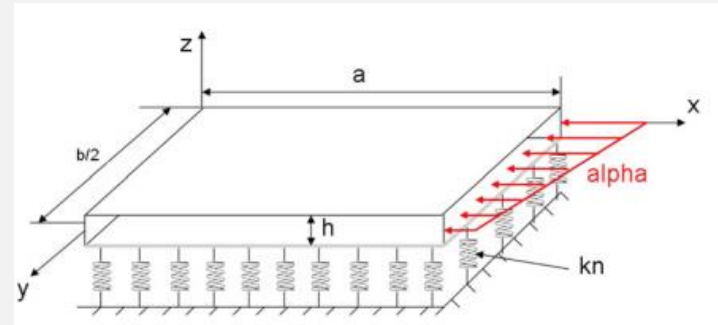


- The main reason for wrinkling occurrence is the mismatch in length between the prescribed path on the surface and the actual delivered tow from the machine head.
- This mismatch in length can be detected during the design phase, hence the possibility of improvement.

Wrinkling in the Literature

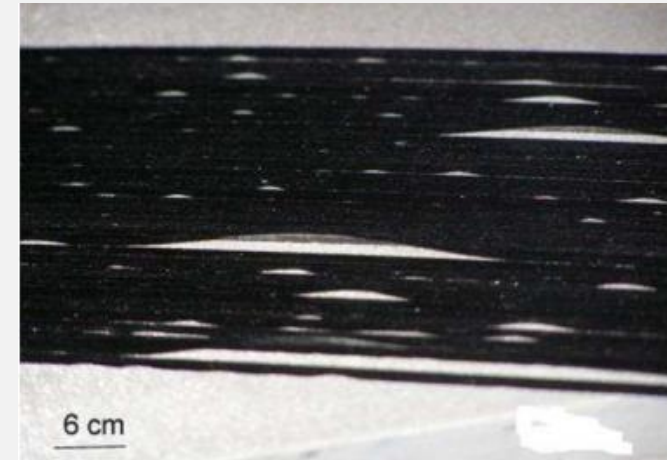


Most common tow steering defect [2]

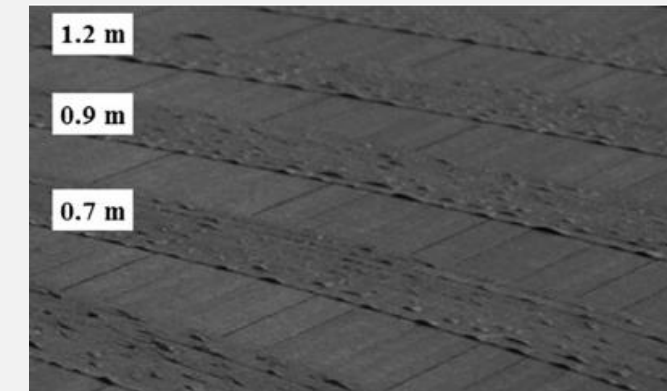


Wrinkling model: Buckling of plate on elastic foundation[2]

- [1] tow buckling occurs on the inside radius of the tow if the compressive forces are too high, and tow pull-up (or folding) occurs on the outside radius of the tow due to tensile forces.
- [2] and [3] use a buckling analysis applied to a tow during AFP based on the model of an orthotropic plate laying on elastic foundation



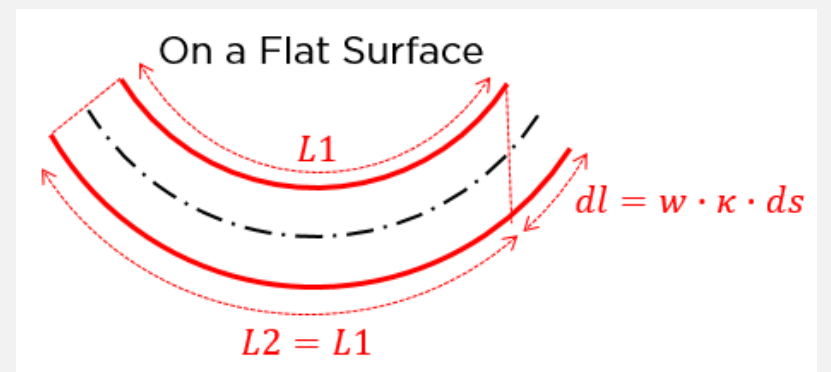
Buckling of steered prepreg tows [1]



Wrinkles in steered dry fiber [3]

Modeling Approach

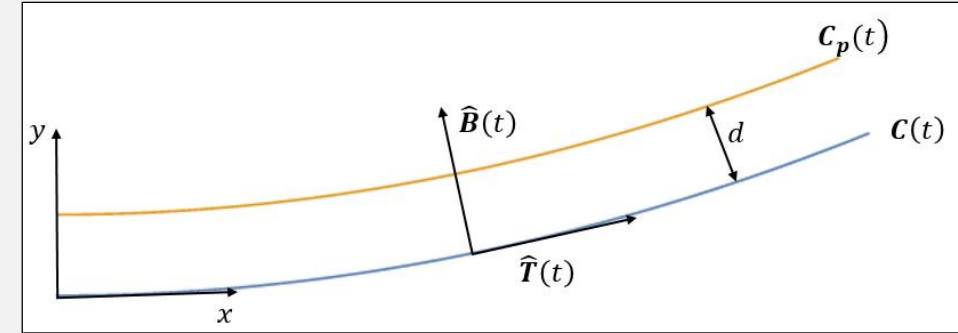
- The stability analysis based on finite size plate-like element assumption is abandoned in favor of a functional form of the tow-path with finite width
- 0th Order
 - Ignore elasticity, viscoelasticity, and tackiness
 - Assume the slit tape to be a membrane with large in-plane stiffness but small bending stiffness
- 1st Order
 - Include elastic deformations
- 2nd Order
 - Include viscoelastic and nonlinear deformations.



Tow-Path Modeling on Flat Surface

- In 2D: the boundary curves are generated by following the normal vector to the original path $C(t)$ using the following equation:

$$C(t) : \begin{cases} x(t) = u_c(t) \\ y(t) = v_c(t) \end{cases}, \quad C_p(t) : \begin{cases} x_p(t) = u_c(t) - d \hat{v}'_c(t) \\ y_p(t) = v_c(t) + d \hat{u}'_c(t) \end{cases}$$



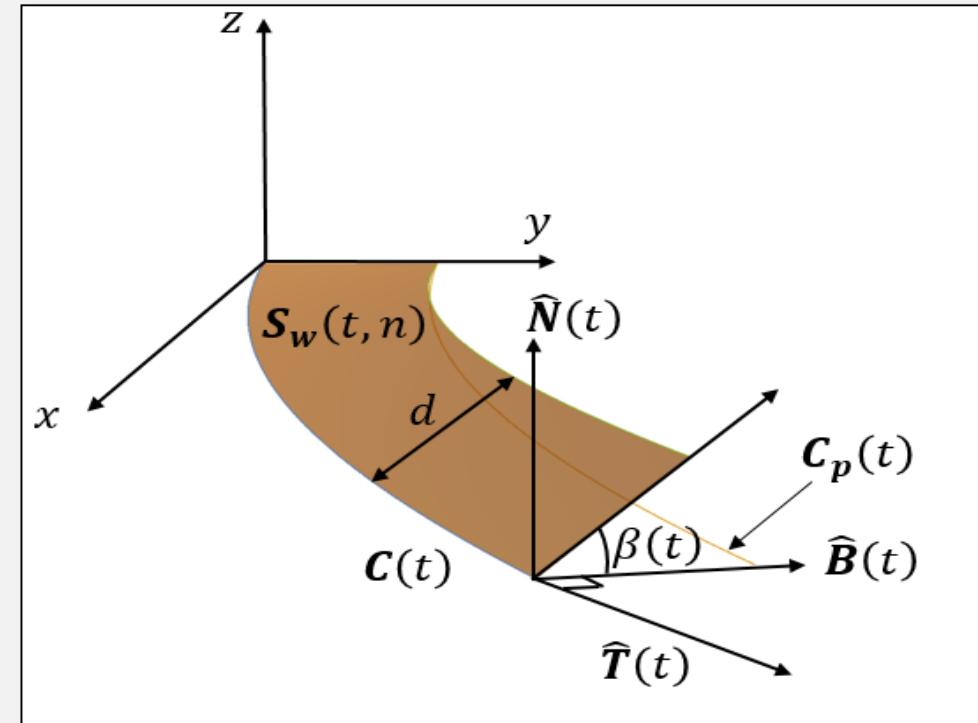
- Since the two sides of the paths have different length, the tow will lift up from the shorter side and buckle. The shape of the buckle is assumed to be a cosine function similar to a clamped beam.

$$S_w(t, n) = \begin{cases} x_w(t, n) = u_c(t) - n d \hat{v}'_c(t) \cos(\beta(t)) \\ y_w(t, n) = v_c(t) + n d \hat{u}'_c(t) \cos(\beta(t)) \\ z_w(t, n) = n d \sin(\beta(t)) \end{cases}$$

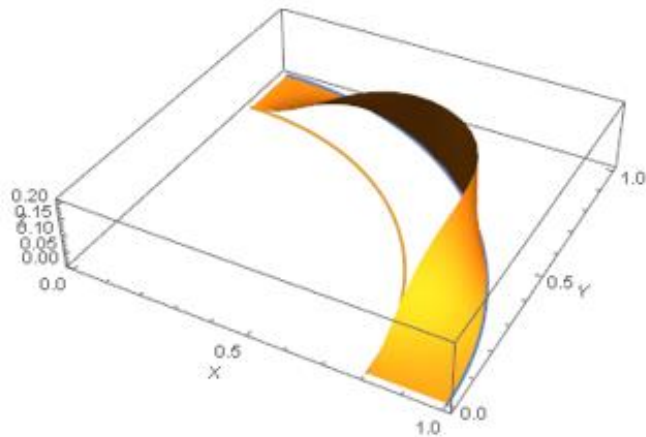
$$\beta(t) = k \left(1 - \cos \left(\frac{2\pi(t - t_{i-1})}{t_i - t_{i-1}} \right) \right)$$

$$\int_{t_{i-1}}^{t_i} \sqrt{\left(\frac{dx}{dt}\right)^2 + \left(\frac{dy}{dt}\right)^2} dt = \int_{t_{i-1}}^{t_i} \sqrt{\left(\frac{dx_w}{dt}\right)^2 + \left(\frac{dy_w}{dt}\right)^2 + \left(\frac{dz_w}{dt}\right)^2} dt = \frac{L}{N}$$

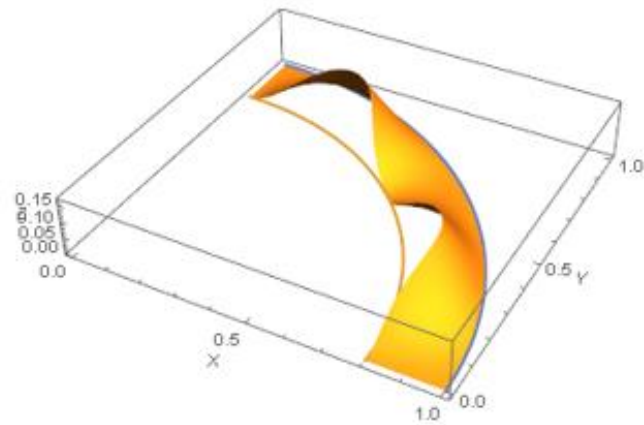
for $i = 1, \dots, N$.



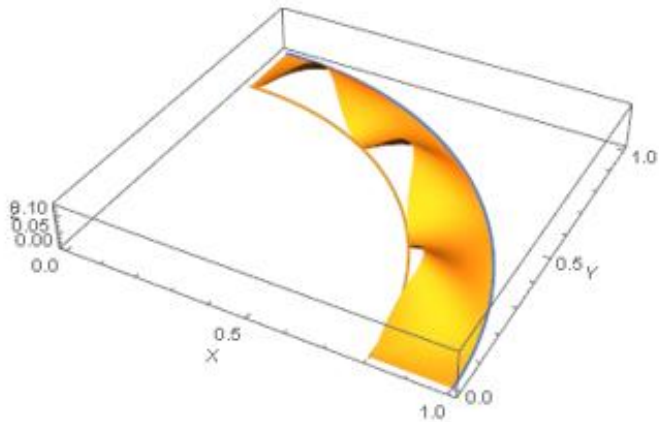
Results for a circular arc



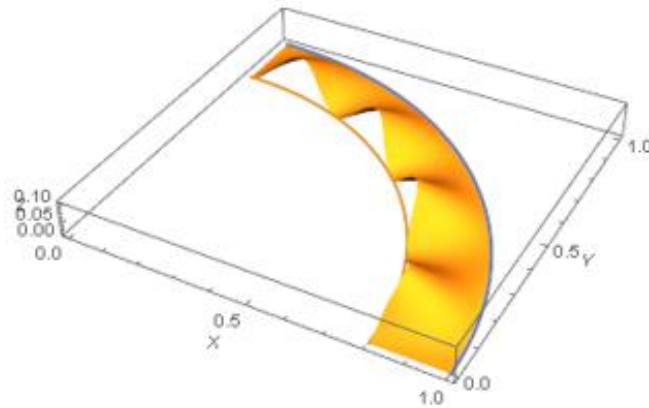
(a) $N = 1$ wrinkle



(b) $N = 2$ wrinkles



(c) $N = 3$ wrinkles



(d) $N = 4$ wrinkles

- The following reference path is defined:

$$C(t) = \{\cos t, \sin t\} \quad , \quad 0 \leq t \leq \pi/2$$

$$w = 0.1 \quad (\text{non dimensional units})$$

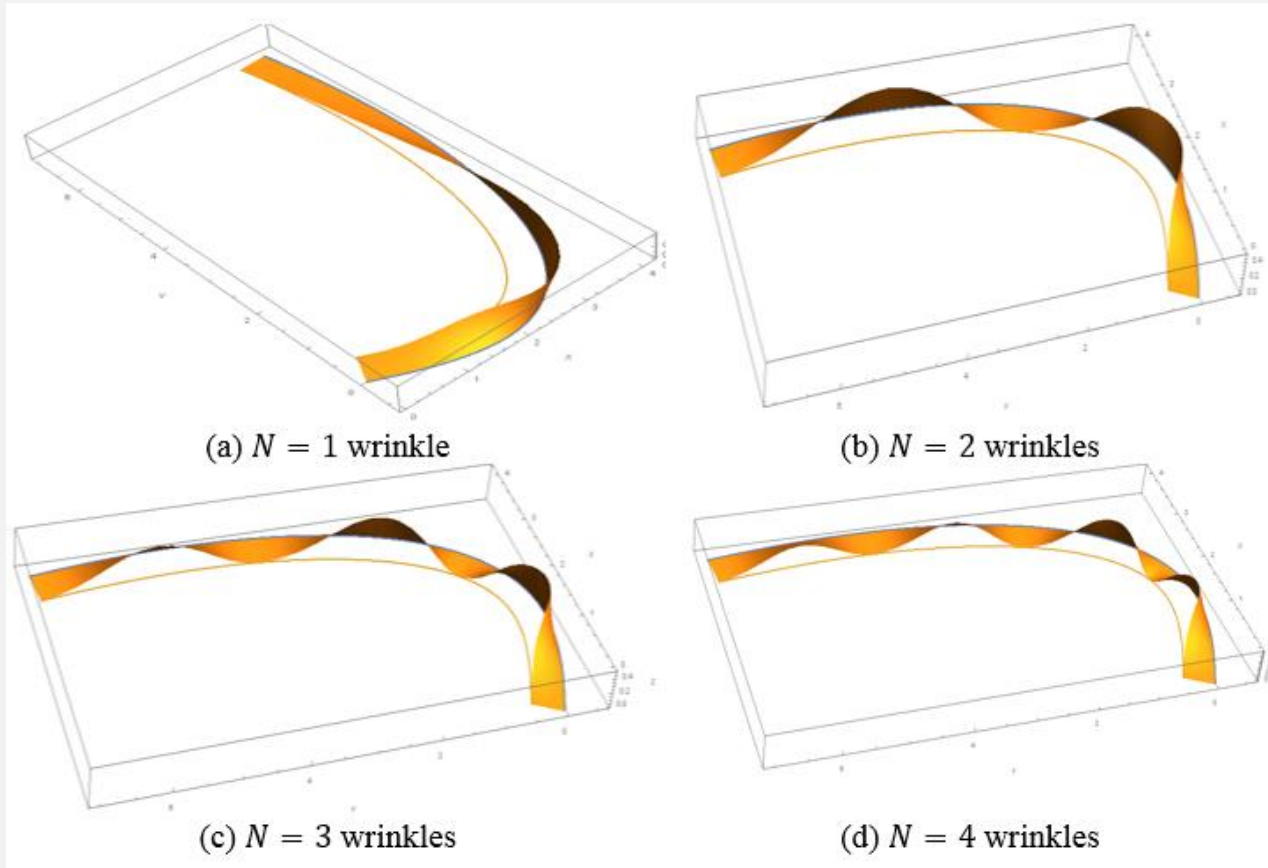
$$\kappa = 1 \quad (\text{constant curvature})$$

Analysis:

- As the number of wrinkles increases the amplitude decreases.
- The amplitude of the wrinkles is proportional to the curvature.
- Higher number of wrinkles can be obtained at higher energy level

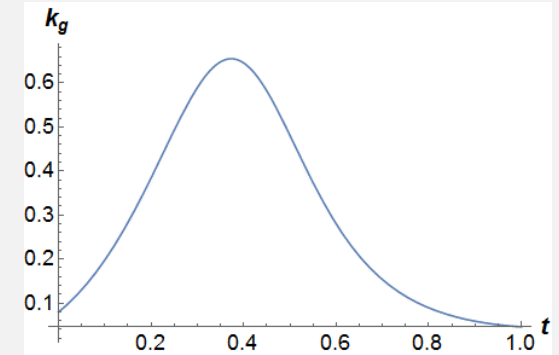
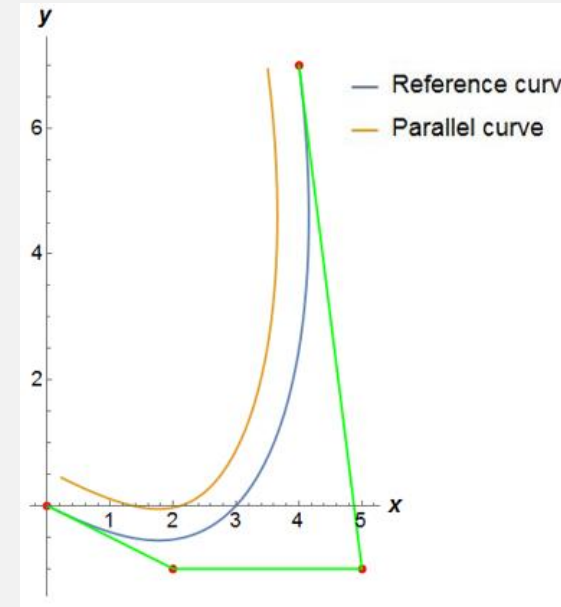


Results for a curvilinear NURBS path



Analysis:

- As the number of wrinkles increases the amplitude decreases.
- The amplitude of the wrinkles is proportional to the curvature.



A random curvilinear path is defined in NURBS form with the following parameters:

$$P_i = \{(0, 0), (2, -1), (5, -1), (4, 7)\},$$

$$w_i = \{1, 1.5, 1, 1\}.$$

$$KV = \{0, 0, 0, 0, 1, 1, 1, 1\},$$

$$p = 3 \quad \text{and} \quad w = 0.5$$



Tow-Path Modeling on General Surfaces

- Start by defining a surface in parametric form:

$$\mathbf{S}(u, v) = X(u, v)\hat{i} + Y(u, v)\hat{j} + Z(u, v)\hat{k} \quad ,$$

- Compute the unit tangents and normal vectors to the surface:

$$\hat{\mathbf{S}}_u(u, v) = \frac{\partial \mathbf{S}(u, v) / \partial u}{\|\partial \mathbf{S}(u, v) / \partial u\|} \quad , \quad \hat{\mathbf{S}}_v(u, v) = \frac{\partial \mathbf{S}(u, v) / \partial v}{\|\partial \mathbf{S}(u, v) / \partial v\|} \quad ,$$

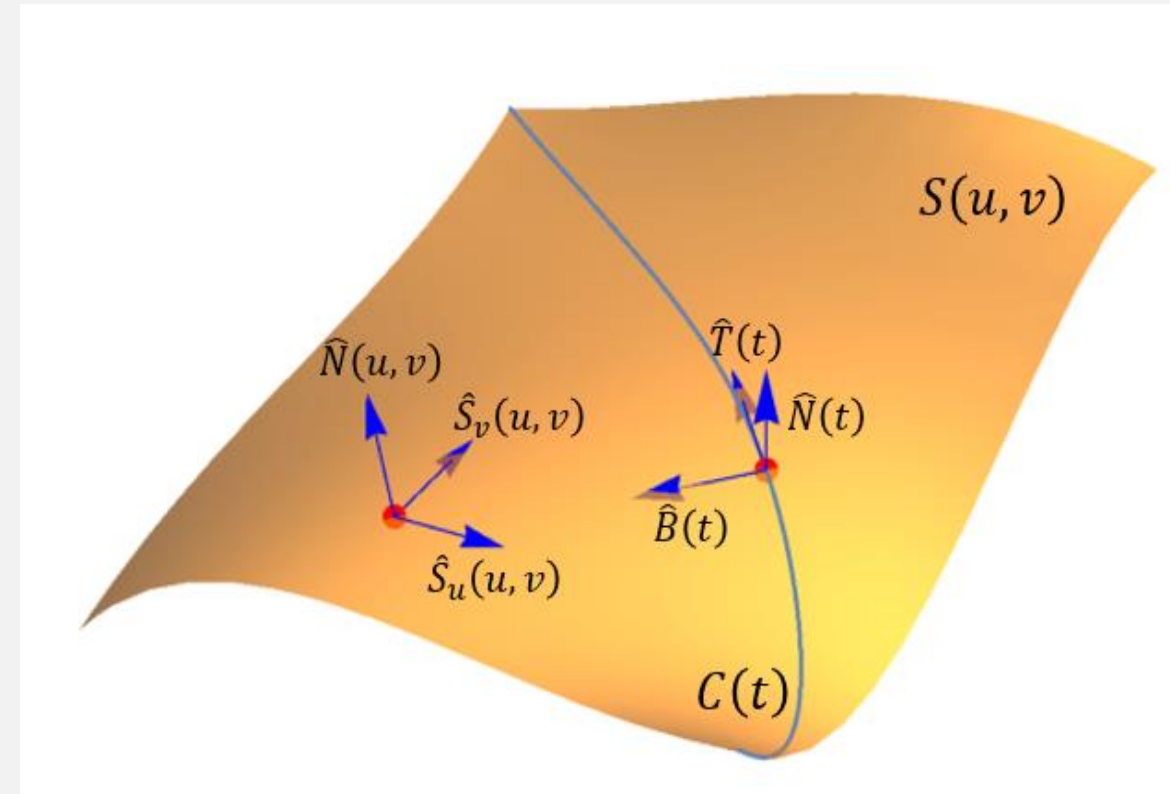
$$\hat{\mathbf{N}}(u, v) = \hat{\mathbf{S}}_u \times \hat{\mathbf{S}}_v$$

- Define an arbitrary path on the surface:

$$\mathbf{C}(t) = \mathbf{S}(u_c(t), v_c(t))$$

- Compute the path tangent, normal, and binormal vectors:

$$\hat{\mathbf{T}}(t) = \frac{d\mathbf{C}(t)/dt}{\|d\mathbf{C}(t)/dt\|} \quad , \quad \hat{\mathbf{B}}(t) = \hat{\mathbf{N}}(t) \times \hat{\mathbf{T}}(t) .$$

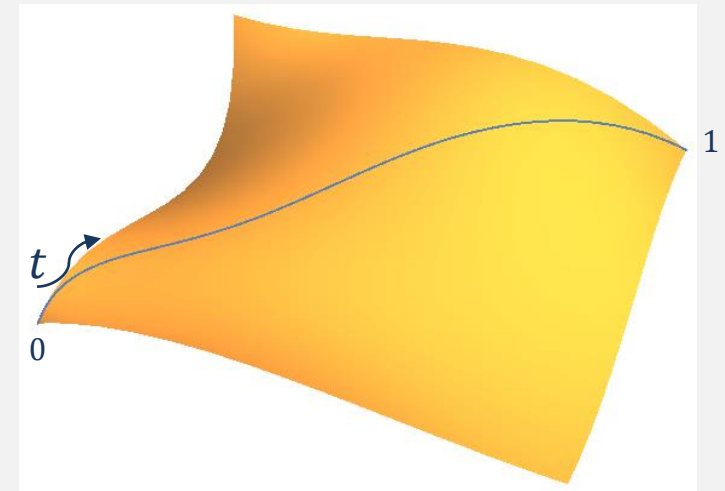
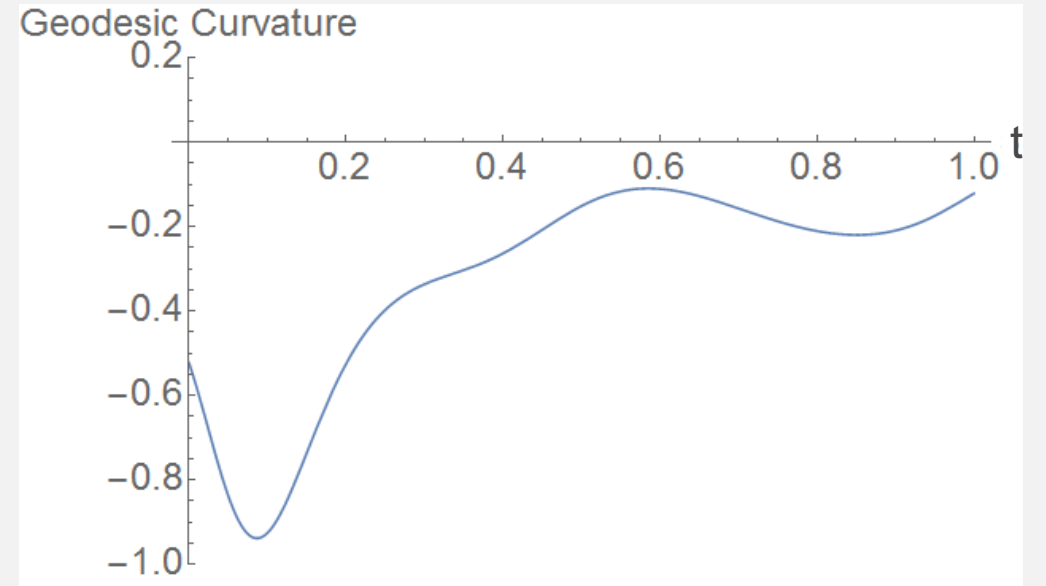


Geodesic Curvature

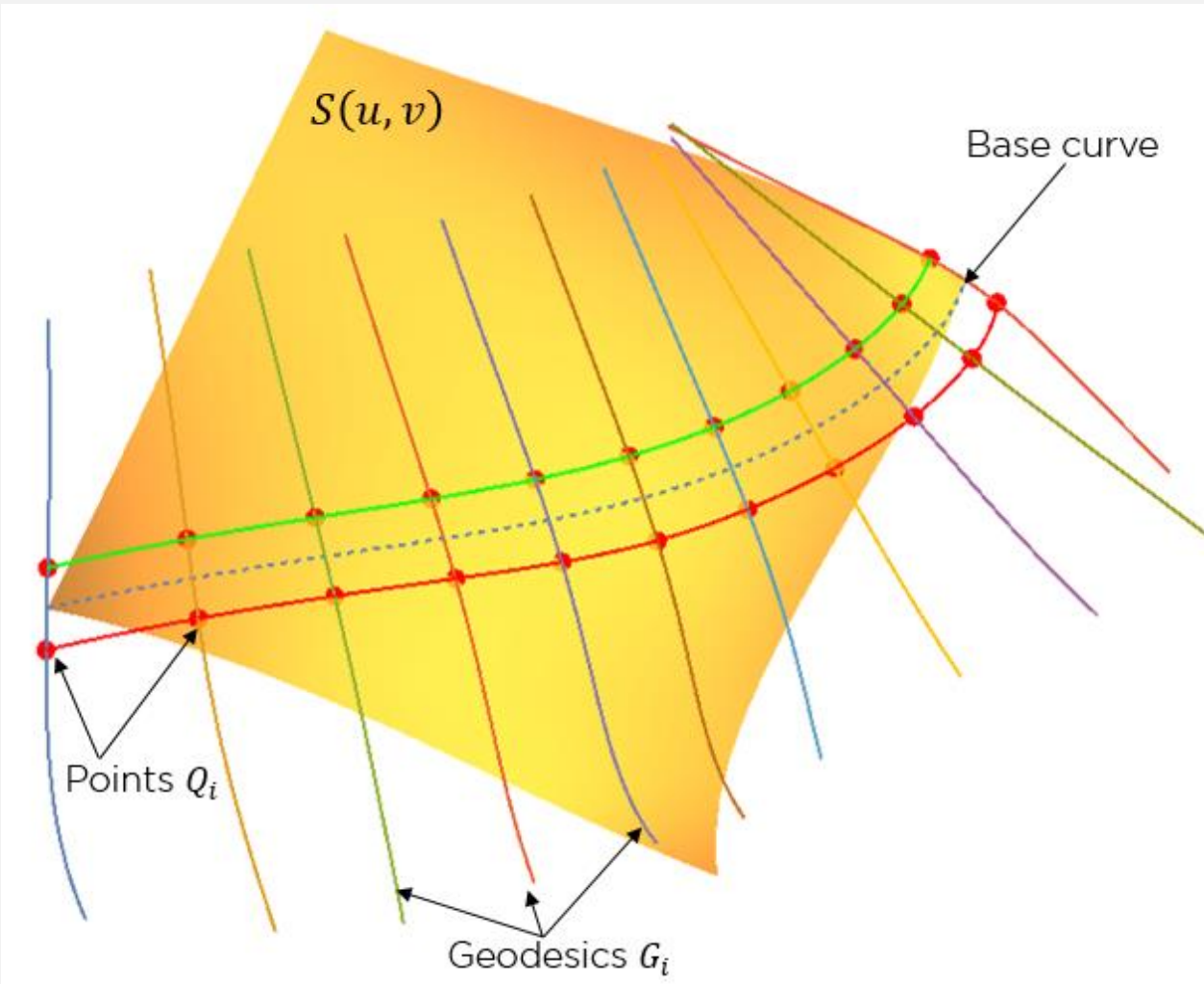
- An important feature of the path along the surface is the geodesic curvature. It has a similar physical meaning of the curvature of a curve in 2D.

$$k_g = \frac{\sqrt{EG - F^2} \left[-\Gamma_{11}^2 u_c'^3 + \Gamma_{22}^1 v_c'^3 - (2\Gamma_{12}^2 - \Gamma_{11}^1) u_c'^2 v_c' + (2\Gamma_{12}^1 - \Gamma_{22}^2) u_c' v_c'^2 + u_c'' v_c' - v_c'' u_c' \right]}{\left(E u_c'^2 + 2F u_c' v_c' + G v_c'^2 \right)^{\frac{3}{2}}}$$

- E, F and G: first fundamental coefficients
- Γ_{ij}^k : Christoffel symbols
- u, v path parameters



Parallel Curves on the Surface



Algorithm:

- Take n points P_i along the base curve: $P_i = \{P_1, P_2, \dots, P_n\}$, $i = 1 \dots n$
- Find each geodesic G_i starting at P_i in the direction orthogonal to the base curve
- Find the points Q_i on the geodesics at a distance d_i equal to the tow width
- Generate the parallel path by interpolating the points Q_i

Geodesic paths can be found by solving the following system:

$$\begin{cases} u'' + \Gamma_{11}^1 u'^2 + 2\Gamma_{12}^1 u'v' + \Gamma_{22}^1 v'^2 = 0 \\ v'' + \Gamma_{11}^2 u'^2 + 2\Gamma_{12}^2 u'v' + \Gamma_{22}^2 v'^2 = 0 \end{cases}$$



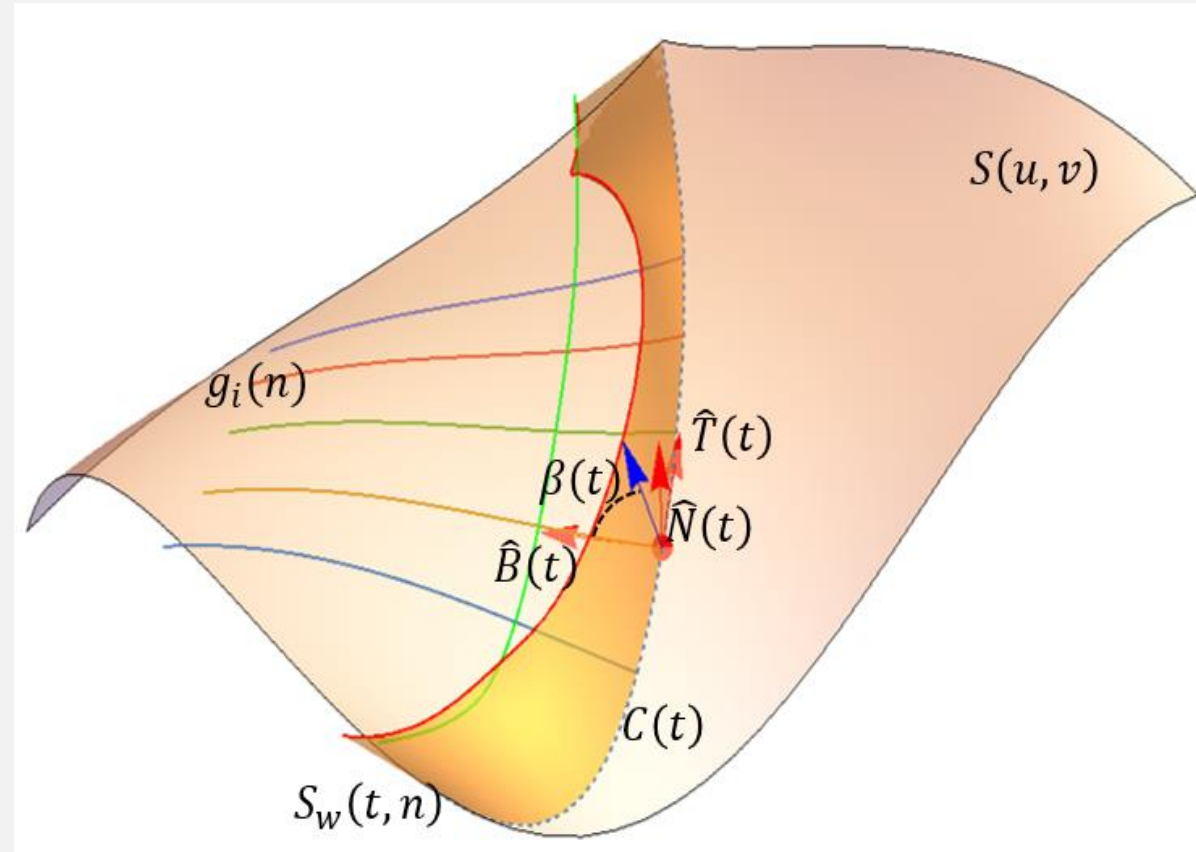
Wrinkles on General Surfaces

- A similar approach to the 2D path is used to find the wrinkled shape by following a rotational motion around the reference path:

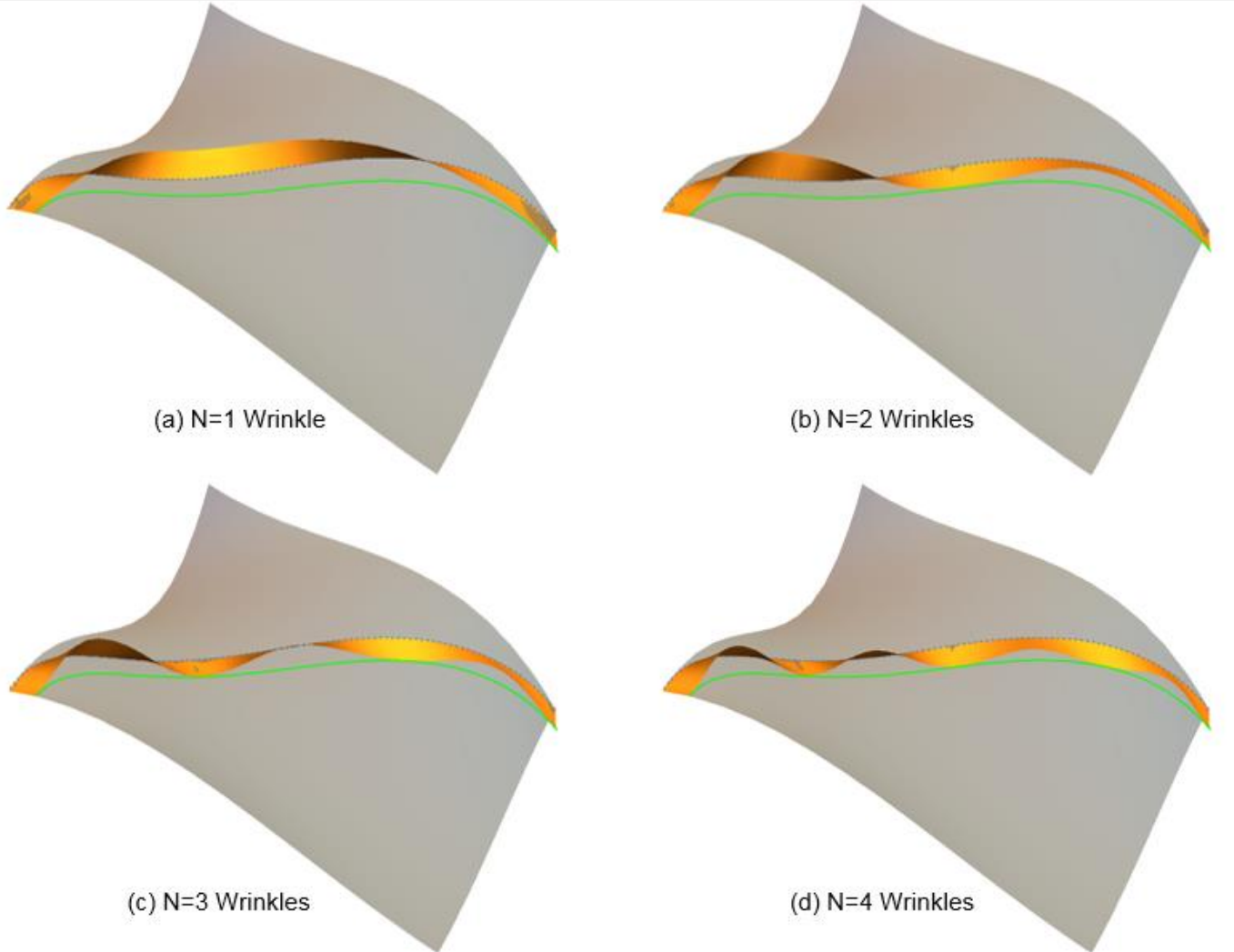
$$\mathbf{S}_w(t, n) = (\mathbf{S}_{tow}(t, n) - \mathbf{S}_{tow}(t, 0)) \cdot \mathcal{R}(\hat{\mathbf{T}}(t), \beta(t)) + \mathbf{S}_{tow}(t, 0)$$

$$\beta(t) = k \left(1 - \cos \left(\frac{2\pi(t - t_0)}{t_1 - t_0} \right) \right)$$

$$\int_{t_{i-1}}^{t_i} \sqrt{E \left(\frac{du_c}{dt} \right)^2 + F \frac{du_c}{dt} \frac{dv_c}{dt} + G \left(\frac{dv_c}{dt} \right)^2} dt = \frac{L}{N}, \quad \text{for } i = 1, \dots, N.$$

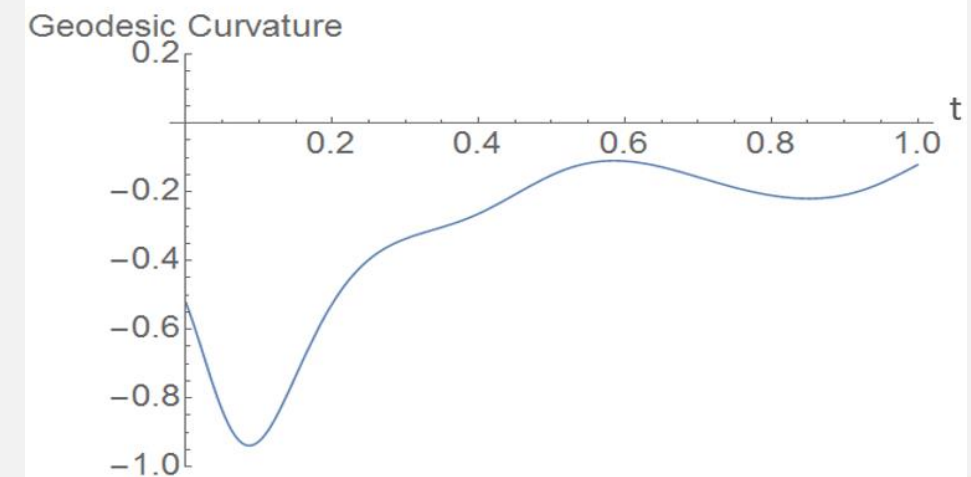


Results for General Surfaces

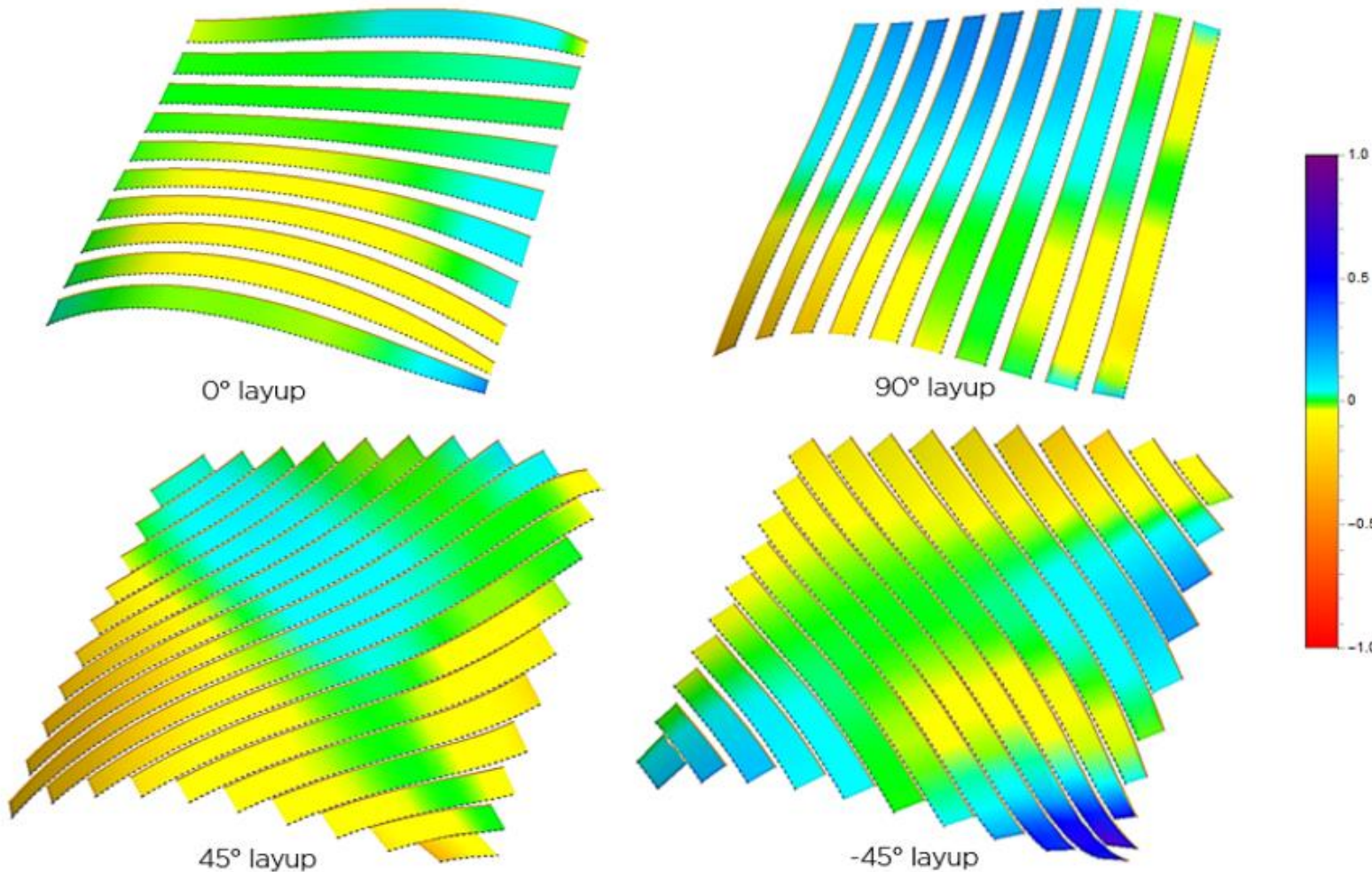


- **Analysis:**

- As the number of wrinkles increases the amplitude decreases.
- The amplitude of the wrinkles is proportional to the geodesic curvature.



Wrinkling Color Map



- Positive areas mean that possible wrinkles might appear on the dashed side of the tow
- Negative areas mean that possible wrinkles might appear on the solid side of the tow
- Different layups have different critical regions



Conclusion & Future Work

- A tow-path based formulation for wrinkling is developed and implemented for flat and general surfaces
- The shape of the wrinkles is assumed to be a cosine function, and it was found that the amplitude is proportional to the curvature
- A color map for different layups is presented to detect possible regions of wrinkling
- Next Steps:
 - Include material properties and elastic deformations (1st order)
 - Include viscoelastic and non-linear deformations (2nd order)



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